

## SBML Model Report

# Model name: “Goldbeter1991 - Min Mit Oscil, Expl Inact”



May 6, 2016

## 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Bruce Shapiro<sup>1</sup> at February eighth 2005 at 5:34 p. m. and last time modified at December eleventh 2012 at 3:30 p. m. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	5
events	0	constraints	0
reactions	7	function definitions	0
global parameters	5	unit definitions	0
rules	2	initial assignments	0

## Model Notes

Goldbeter1991 - Min Mit Oscil, Expl Inact

This model represents the inactive forms of CDC-2 Kinase and Cyclin Protease as separate species, unlike the ODEs in the published paper, in which the equations for the inactive forms are substituted into the equations for the active forms using a mass conservation rule

<sup>1</sup>NASA Jet Propulsion Laboratory, [bshapiro@jpl.nasa.gov](mailto:bshapiro@jpl.nasa.gov)

$M+MI=1, X+XI=1$ . Mass is still conserved in this model through the explicit reactions  $M \rightleftharpoons MI$  and  $X \rightleftharpoons XI$ . The terms in the kinetic laws are identical to the corresponding terms in the kinetic laws in the published paper.

This model has been generated by MathSBML 2.4.6 (14-January-2005) 14-January-2005 18:37:35.503857.

This model is described in the article: [A minimal cascade model for the mitotic oscillator involving cyclin and cdc2 kinase](#). Goldbeter A. Proc. Natl. Acad. Sci. USA 1991 Oct; 88(20):9107-11

Abstract:

A minimal model for the mitotic oscillator is presented. The model, built on recent experimental advances, is based on the cascade of post-translational modification that modulates the activity of cdc2 kinase during the cell cycle. The model pertains to the situation encountered in early amphibian embryos, where the accumulation of cyclin suffices to trigger the onset of mitosis. In the first cycle of the bicyclic cascade model, cyclin promotes the activation of cdc2 kinase through reversible dephosphorylation, and in the second cycle, cdc2 kinase activates a cyclin protease by reversible phosphorylation. That cyclin activates cdc2 kinase while the kinase triggers the degradation of cyclin has suggested that oscillations may originate from such a negative feedback loop [Flix, M. A., Labb, J. C., Dore, M., Hunt, T. & Karsenti, E. (1990) Nature (London) 346, 379-382]. This conjecture is corroborated by the model, which indicates that sustained oscillations of the limit cycle type can arise in the cascade, provided that a threshold exists in the activation of cdc2 kinase by cyclin and in the activation of cyclin proteolysis by cdc2 kinase. The analysis shows how mitotic oscillations may readily arise from time lags associated with these thresholds and from the delayed negative feedback provided by cdc2-induced cyclin degradation. A mechanism for the origin of the thresholds is proposed in terms of the phenomenon of zero-order ultrasensitivity previously described for biochemical systems regulated by covalent modification.

This model is hosted on [BioModels Database](#) and identified by: [BIOMD0000000004](#) .

To cite BioModels Database, please use: [BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models](#) .

To the extent possible under law, all copyright and related or neighbouring rights to this encoded model have been dedicated to the public domain worldwide. Please refer to [CC0 Public Domain Dedication](#) for more information.

## 2 Unit Definitions

This is an overview of five unit definitions which are all predefined by SBML and not mentioned in the model.

### 2.1 Unit substance

**Notes** Mole is the predefined SBML unit for substance.

**Definition** mol

## 2.2 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** l

## 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

## 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

## 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
cell	cell		3	1	litre	<input checked="" type="checkbox"/>	

### 3.1 Compartment cell

This is a three dimensional compartment with a constant size of one litre.

**Name** cell

## 4 Species

This model contains five species. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
C	Cyclin	cell	$\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
M	Active CDC-2 Kinase	cell	$\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
X	Active Cyclin Protease	cell	$\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
MI	Inactive CDC-2 Kinase	cell	$\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$
XI	Inactive Cyclin Protease	cell	$\text{mol} \cdot \text{l}^{-1}$	$\square$	$\square$

## 5 Parameters

This model contains five global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V1	V1		0.0		<input type="checkbox"/>
V3	V3		0.0		<input type="checkbox"/>
VM1	VM1		3.0		<input checked="" type="checkbox"/>
VM3	VM3		1.0		<input checked="" type="checkbox"/>
Kc	Kc		0.5		<input checked="" type="checkbox"/>

## 6 Rules

This is an overview of two rules.

### 6.1 Rule V1

Rule V1 is an assignment rule for parameter V1:

$$V1 = [C] \cdot VM1 \cdot ([C] + Kc)^{-1} \quad (1)$$

### 6.2 Rule V3

Rule V3 is an assignment rule for parameter V3:

$$V3 = [M] \cdot VM3 \quad (2)$$

## 7 Reactions

This model contains seven reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	reaction1	creation of cyclin	$\emptyset \longrightarrow C$	
2	reaction2	default degradation of cyclin	$C \longrightarrow \emptyset$	
3	reaction3	cdc2 kinase triggered degradation of cyclin	$C \xrightarrow{X} \emptyset$	
4	reaction4	activation of cdc2 kinase	$MI \longrightarrow M$	
5	reaction5	deactivation of cdc2 kinase	$M \longrightarrow MI$	
6	reaction6	activation of cyclin protease	$XI \longrightarrow X$	
7	reaction7	deactivation of cyclin protease	$X \longrightarrow XI$	

## 7.1 Reaction `reaction1`

This is an irreversible reaction of no reactant forming one product.

**Name** creation of cyclin

### Reaction equation



### Product

Table 6: Properties of each product.

Id	Name	SBO
C	Cyclin	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_1 = \text{vol}(\text{cell}) \cdot v_i \quad (4)$$

Table 7: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
<code>v<sub>i</sub></code>			0.025		<input checked="" type="checkbox"/>

## 7.2 Reaction `reaction2`

This is an irreversible reaction of one reactant forming no product.

**Name** default degradation of cyclin

### Reaction equation



### Reactant

Table 8: Properties of each reactant.

Id	Name	SBO
C	Cyclin	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_2 = [C] \cdot \text{vol}(\text{cell}) \cdot \text{kd} \quad (6)$$

Table 9: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
kd			0.01		<input checked="" type="checkbox"/>

### 7.3 Reaction `reaction3`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

**Name** cdc2 kinase triggered degradation of cyclin

### Reaction equation



### Reactant

Table 10: Properties of each reactant.

Id	Name	SBO
C	Cyclin	

### Modifier

Table 11: Properties of each modifier.

Id	Name	SBO
X	Active Cyclin Protease	



## Kinetic Law

**Derived unit** contains undeclared units

$$v_3 = [C] \cdot \text{vol}(\text{cell}) \cdot v_d \cdot [X] \cdot ([C] + K_d)^{-1} \quad (8)$$

Table 12: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
v <sub>d</sub>			0.25		<input checked="" type="checkbox"/>
K <sub>d</sub>			0.02		<input checked="" type="checkbox"/>

## 7.4 Reaction `reaction4`

This is an irreversible reaction of one reactant forming one product.

**Name** activation of cdc2 kinase

### Reaction equation



### Reactant

Table 13: Properties of each reactant.

Id	Name	SBO
MI	Inactive CDC-2 Kinase	

### Product

Table 14: Properties of each product.

Id	Name	SBO
M	Active CDC-2 Kinase	

## Kinetic Law

**Derived unit** contains undeclared units

$$v_4 = \text{vol}(\text{cell}) \cdot [\text{MI}] \cdot V_1 \cdot (K_1 + [\text{MI}])^{-1} \quad (10)$$

Table 15: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
K1			0.005		<input checked="" type="checkbox"/>

## 7.5 Reaction `reaction5`

This is an irreversible reaction of one reactant forming one product.

**Name** deactivation of cdc2 kinase

### Reaction equation



### Reactant

Table 16: Properties of each reactant.

Id	Name	SBO
M	Active CDC-2 Kinase	

### Product

Table 17: Properties of each product.

Id	Name	SBO
MI	Inactive CDC-2 Kinase	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_5 = \text{vol}(\text{cell}) \cdot [M] \cdot V_2 \cdot (K_2 + [M])^{-1} \quad (12)$$

Table 18: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
V2			1.500		<input checked="" type="checkbox"/>
K2			0.005		<input checked="" type="checkbox"/>

## 7.6 Reaction `reaction6`

This is an irreversible reaction of one reactant forming one product.

**Name** activation of cyclin protease

### Reaction equation



### Reactant

Table 19: Properties of each reactant.

Id	Name	SBO
XI	Inactive Cyclin Protease	

### Product

Table 20: Properties of each product.

Id	Name	SBO
X	Active Cyclin Protease	

### Kinetic Law

**Derived unit** contains undeclared units

$$v_6 = \text{vol}(\text{cell}) \cdot V_3 \cdot [\text{XI}] \cdot (\text{K3} + [\text{XI}])^{-1} \quad (14)$$

Table 21: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
K3			0.005		<input checked="" type="checkbox"/>

## 7.7 Reaction `reaction7`

This is an irreversible reaction of one reactant forming one product.

**Name** deactivation of cyclin protease

## Reaction equation



## Reactant

Table 22: Properties of each reactant.

Id	Name	SBO
X	Active Cyclin Protease	

## Product

Table 23: Properties of each product.

Id	Name	SBO
XI	Inactive Cyclin Protease	

## Kinetic Law

**Derived unit** contains undeclared units

$$v_7 = \text{vol}(\text{cell}) \cdot V_4 \cdot [X] \cdot (K_4 + [X])^{-1} \quad (16)$$

Table 24: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
K4			0.005		<input checked="" type="checkbox"/>
V4			0.500		<input checked="" type="checkbox"/>

## 8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to

false and `spacialDimensions > 0` for certain species.

### 8.1 Species C

**Name** Cyclin

**Initial concentration**  $0.01 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [reaction2](#), [reaction3](#) and as a product in [reaction1](#)).

$$\frac{d}{dt}C = v_1 - v_2 - v_3 \quad (17)$$

### 8.2 Species M

**Name** Active CDC-2 Kinase

**Initial concentration**  $0.01 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [reaction5](#) and as a product in [reaction4](#)).

$$\frac{d}{dt}M = v_4 - v_5 \quad (18)$$

### 8.3 Species X

**Name** Active Cyclin Protease

**Initial concentration**  $0.01 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [reaction7](#) and as a product in [reaction6](#) and as a modifier in [reaction3](#)).

$$\frac{d}{dt}X = v_6 - v_7 \quad (19)$$

### 8.4 Species MI

**Name** Inactive CDC-2 Kinase

**Initial concentration**  $0.99 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [reaction4](#) and as a product in [reaction5](#)).

$$\frac{d}{dt}MI = v_5 - v_4 \quad (20)$$

## 8.5 Species XI

**Name** Inactive Cyclin Protease

**Initial concentration**  $0.99 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [reaction6](#) and as a product in [reaction7](#)).

$$\frac{d}{dt}\text{XI} = v_7 - v_6 \quad (21)$$

SBML<sup>2</sup>LaTeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

<sup>a</sup>Center for Bioinformatics Tübingen (ZBIT), Germany

<sup>b</sup>California Institute of Technology, Beckman Institute BNMC, Pasadena, United States

<sup>c</sup>European Bioinformatics Institute, Wellcome Trust Genome Campus, Hinxton, United Kingdom

<sup>d</sup>EML Research gGmbH, Heidelberg, Germany